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Predicting Systematic Risk: Implications from Growth Options^{*}

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Résumé

En vertu de l'effet de levier financier bien connu, les baisses du cours des actions produisent une hausse du bêta des capitaux propres avec facteur d'endettement par rapport à un bêta donné des capitaux propres sans facteur d'endettement. Toutefois, étant donné que les options de croissance sont plus volatiles et présentent un risque plus élevé que les actifs en place, une baisse de leur prix peut contribuer à diminuer le bêta des capitaux propres sans facteur d'endettement à cause de l'effet de « levier d'exploitation ». Ce phénomène s'explique par le fait que les baisses de prix peuvent être associées à une perte proportionnellement plus élevée dans le cas des options de croissance par rapport aux actifs en place. La plupart des études existantes mettent l'accent sur l'effet de levier financier. Le document actuel se penche sur les deux effets. Nos résultats empiriques démontrent que, contrairement à la croyance répandue, l'effet de levier d'exploitation domine largement l'effet de levier financier, même dans le cas des firmes dont le facteur d'endettement est élevé et qui, vraisemblablement, ont peu d'options de croissance. Nous établissons un lien entre les variations dans les bêtas et les caractéristiques mesurables des firmes qui représentent la proportion investie dans les options de croissance. Nous démontrons que ces données indirectes prédisent conjointement une forte proportion de différences transversales dans les bêtas. Les résultats ont une incidence importante sur la prévisibilité des bêtas des capitaux propres et, par le fait même, sur la fixation empirique des prix des actifs et sur l'optimisation du portefeuille qui limite le risque systématique.

Mots clés : effet de levier financier, options de croissance, risque

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Abstract

Via the well-known financial leverage effect, decreases in stock prices cause an increase in the levered equity beta for a given unlevered equity beta. However, as growth options are more volatile and have higher risk than assets in place, a price decrease may decrease the unlevered equity beta via an "operating leverage" effect. This is because decreases in prices can be associated with a proportionately higher loss in growth options than in assets in place. Most of the existing literature focuses on the financial leverage effect. This paper examines both effects. Our empirical results show that, contrary to common belief, the operating leverage effect largely dominates the financial leverage effect, even for highly levered firms that presumably have few growth options. We link variations in betas to measurable firm characteristics that proxy for the proportion of the firm invested in growth options. We show that these proxies jointly predict a large fraction of cross-sectional differences in betas. These results have important implications on the predictability of equity betas, hence on empirical asset pricing and on portfolio optimization that controls for systematic risk.

Keywords: financial leverage effect, growth options, risk

1 Introduction

The measurement of systematic risk (beta) is essential for portfolio and risk management in addition to tests of asset pricing models of risk versus return and market efficiency. Various anomalies recently appeared in the academic literature have triggered a renewed interest in the determinants of systematic risk. The proper measurement of systematic risk is central for the study of the various anomalies, mutual and hedge fund performance.

Consider for example, DeBondt and Thaler (1985) who show that long term winners (losers) perform poorly (well) over the following three to five year period. They argue that the observed reversal pattern supports the hypothesis that stock prices tend to overreact to information. However, Chan (1988), Ball and Kothari (1989) and others, argue that the higher subsequent returns of the losers are likely to be due to increased systematic risk. In effect, they invoke the original financial leverage hypothesis in Hamada (1972) and Rubinstein (1974), whereby losses in equity value result in higher levered equity betas through an increase in financial leverage. DeBondt and Thaler (1987) and Chopra et al. (1992) counter that such changes in beta cannot explain the asymmetry in return reversals, where the subsequent loss of past winners is far smaller than the subsequent gain of past losers. Further, and in sharp contrast with this financial leverage hypothesis, we will see below that losses of growth options actually lead to lower equity betas for the losers. This shows that operating leverage effects dominate financial leverage. Despite the intense debate on the nature of the well publicized reversal results, this latter possibility is not explored in the empirical literature.

To understand performance one must first consider how betas change. This is especially crucial for extreme performers. Ex-ante determinants of systematic risk initially received attention in the finance literature.¹ However, most of the current empirical asset pricing and portfolio literature uses simple time series methods such as rolling windows or other univariate filters. In contrast, this paper links, mostly in the cross-section, variations in betas to financial and operating leverage.²

¹Early papers include Beaver et al. (1970), Rosenberg and McKibben (1973) and Rosenberg (1974,1985).

 $^{^{2}}$ Braun et al.(1995) incorporate financial leverage on a GARCH model of time varying betas with mixed results. Cao, Simin and Zhao (2007) study the implications of growth options on the time series of idiosyncratic risk.

To demonstrate the implications of growth options on betas through the operating leverage effect, section 2 discusses a simple model where the firm has growth options and assets in place. The beta of the firm is then a weighted average of the (unlevered) betas of growth options and assets in place. Growth options require more future discretionary investment expenditures than assets in place. So they are akin to out-of-the money options, and hence have higher betas. Then, a decrease in the value of the underlying assets on which the firm has these options, has a stronger impact on growth options than on assets in place. In turn this will decrease the fraction of the total value accounted by growth options. By this "change-in-mix" effect, a decrease in the firm's market value is associated with an decrease in its asset beta. However, there is a second, offsetting effect: A decrease in "moneyness" causes the betas of all the options in the firm to increase as the value of the underlying asset decreases. The model implies that, for a plausible range of ratios of growth opportunities to assets in place, the "change-in-mix" effect dominates the "moneyness" effect. The well known financial leverage effect also offsets the change-in-mix effect for levered betas.

We then proceed with an empirical analysis. Our results show that the "change-in-mix" effect also dominates financial leverage. Specifically, we find that betas are highly related to proxies for the fraction of the firms' assets in growth options. First, after long-term changes in stock prices, the levered equity betas of losers decrease and those of winners increase. This is consistent with the conclusion of Chopra et al. (1992) that the patterns of change in the betas of winners and losers contradict the financial leverage hypothesis. We find that these results are robust to the initial financial leverage. Namely, even firms with initial high leverage and low growth options experience decreases in betas after losses. Note that the patterns in levered equity betas which we uncover allow us to infer the corresponding changes in unlevered betas without the need for a functional relationship between the two. Second, in a cross-sectional analysis, we show that firms with higher growth options, measured by proxies, have higher equity betas. Third, we show that, jointly, a number of growth option proxies are reliable predictors of the cross-section of equity betas.

Changes in betas arising from drastic changes in market values raise the question of how fast the market adjusts to them. Indeed, while most market participants understand financial leverage mechanics, implications from real options theory are not so clear to all. For example, investors less familiar with real options theory could initially ascribe a financial leverage effect on the betas of recent losers. Therefore, these loser stock prices would overreact to subsequent index movements if their betas remained too high for too long. Then, only with further information slowly coming to the market, would the implications of the loss in growth options be factored into the equity beta. Our empirical evidence is consistent with this scenario. Specifically, the annual returns of past losers are negatively correlated with the lagged market returns, suggesting that these stocks may have previously over-reacted to contemporaneous market returns.

The paper proceeds as follows. Section 2 discusses a simple option pricing model to illustrate the effect of market returns on asset betas. Section 3 describes the data and the methodology. Section 4 contains the empirical results and analysis. Section 5 concludes.

2 Growth Options and Unlevered Equity Betas

The simple option-pricing model below will show how unlevered betas are likely to respond to changes in firm values. In the model, firms consist of assets already in place and future growth options requiring further investments. As the firm is not required to make these added investments, growth options can be viewed as call options to acquire an asset at an exercise price equal to the required investment.

First, consider the equity value G of a firm with an option to undertake a project of value sand beta β_s , at an investment cost C_G . First, the beta of this opportunity is $\beta_G = \eta_G \beta_s$, where η_G is the elasticity of the option, see Galai and Masulis (1976). Second, we show in the appendix that $\frac{\partial \eta_G}{\partial (s/C_G)}$ is negative. Therefore, given β_s , the growth opportunity beta, β_G , decreases as moneyness increases. This shows that growth options have higher betas than assets in place which are deep in the money options.³

Now consider a firm with a portfolio of both growth options and assets in place.⁴ Specifically,

 $^{^{3}}$ Some evidence supports this view. For example, Skinner (1993) reports that firms with relatively more growth options tend to have higher asset betas.

 $^{^{4}}$ Myers (1977) describes the firm as a combination of assets in place and growth options. The distinction between the two is more of degree than kind. The market value of most assets can be partly attributed to associated call options from discretionary decisions. So, a small fraction of their value may be akin to growth options.

the firm value is $V = V_A + V_G = AN_A + GN_G$, where $A \equiv A(s), G \equiv G(s)$ are the (option) value of an asset in place and a growth opportunity, and N_A, N_G are the number of such options held by the firm.⁵ The asset in place A(s) is a deep in-the-money option with investment cost $C_A \ll s$. Similarly, G(s) is an out-of-the-money option with $C_G > s$ where s is a state variable that determines the value of different investments. For example, s may be related to price of oil and A and G could represent producing oil wells and undeveloped oil property.⁶ In this case, the unlevered equity beta equals:

$$\beta_V = \frac{V_A \beta_A + V_G \beta_G}{V} = \frac{A N_A \beta_A + G N_G \beta_G}{V} \tag{1}$$

We first consider news about N_G and N_A , the scale of the growth options and assets in place. Analysts regularly revise their assessment of N_A and N_G . Since growth options are harder to precisely measure, it is reasonable to assume that N_G is more volatile than N_A , and bad news are likely to be more about N_G than N_A . From (1), it follows that

$$\frac{\partial \beta_v}{\partial N_G} = \frac{GV_A}{V^2} (\beta_G - \beta_A).$$
⁽²⁾

That is, an increase in N_G causes an increase in the asset beta. $\frac{\partial \beta_V}{\partial N_A}$ follows by simply swapping indices A and G in (2). Hence, an increase in N_A causes a decrease in beta. Joint revisions $\Delta N_A, \Delta N_G$ in the same direction have opposite effects on β_V . The combined effect is given by the total derivative of β_V :

$$d\beta_V = \frac{\beta_G - \beta_A}{V^2} \left(GV_A \Delta N_G - AV_G \Delta N_A \right).$$

For example, in the case of joint good news, we obtain the condition:

$$d\beta_V > 0 \iff \frac{\Delta N_G}{\Delta N_A} > \frac{N_G}{N_A}.$$
 (3)

⁵This allows us to distinguish between firms with many deep out-of-the-money options and those with a few slightly out-of-the-money options.

⁶Berk, Green and Naik (1999) model the firm value in terms of fundamental state variables. In their model growth options are explicitly priced as options whose value is affected by state variables, e.g., interest rates, as well as cash flows. Here we let s be exogenous.

Note that (3) can be rewritten in terms of dollar values V_G, V_A . In any case, the ratio of the increases must be larger than the current ratio of growth options over assets in place. For joint bad news, the right hand side of (3) is a condition for $d\beta_V < 0$.

Now consider the effect of news about the value of s, with N_A and N_G unchanged. In an oil analogy, this would be information about the price of oil, not the amount of oil in the ground. Good news about s increases both A and G, but the overall effect on β_V is unclear since β_A and β_G decrease. To see this, we write $\frac{d\beta_V}{ds}$.

$$\frac{d\beta_V}{ds} = \frac{GN_G}{V}\beta'_G + \frac{AN_A}{V}\beta'_A + N_G\frac{\beta_G - \beta_V}{V}G' + N_A\frac{\beta_A - \beta_V}{V}A',$$

where $G', A', \beta'_G, \beta'_A$ are the derivatives of G, A, β_G, β_A with respect to s. Recall that $\beta_i = \eta_i \beta_S$ for i equal to G or A, replace β_V with (1), and it can be shown that

$$\frac{V}{\beta_S}\frac{d\beta_V}{ds} = GN_G\eta'_G + AN_A\eta'_A + \left[\eta_G - \eta_A\right]^2 \frac{N_A N_G A' G' s}{V}.$$
(4)

While the first two terms are negative, the third term is positive.

As the following numerical example illustrates, the sum of these terms can be positive for a wide range of moneyness s/C_G and weights in growth options V_G/V . The example assumes: $C_A = 1, C_G = 100, s \in [2, 90]$. We also assume without loss of generality, $N_A = 1$, a risk free rate of zero and a variance to maturity $\sigma^2 T = 1$. For this range of s, the asset in place is always very far into the money. The growth opportunity is always out of the money even when s is 90. The amount of growth options relative to assets in place held also matters. To cover a wide range in the proportion of firm value, V_G/V , held in growth options, we use three values of $N_G = 5, 10, 20$.

The bottom panel in figure 1 plots the weight of the firm in growth options, V_G/V versus s/C_G , the moneyness of G. The three curves correspond to $N_G = 5, 10, 20$. The plots confirm that these values of N_G bracket a wide range of weights in growth options. For example, for a moneyness ratio s/C_G around 20%, V_G/V varies from 20% to 60%. The key here is that this wide range of values has no effect on the pattern uncovered by the top plot, β_V versus s/C_G .

The three curves in the top panel in figure 1 have the same shape, with only variations in the location of their minimum and maximum. There are three regions. First, on the left, the growth options are very far out of the money, and hence worth very little. There, an increase in s decreases β_V . Second, on the right, when the growth options are getting closer to the money and make a large fraction V_G/V of the firm, an increase in s also decreases β_V . The common link between these two regions is that the firm is actually homogeneous in the type of options held, nearly all in or nearly all out-of-the money. In contrast, in the middle region, an increase in s actually increases β_V . In the middle region, the firm is the most heterogeneous with close to a fifty-fifty mix of V_G and V_A .

To summarize, unlevered equity betas can more plausibly be positively than negatively correlated with firm value. The relation between firm values and betas depend on the mix between growth options and assets in place, the sensitivity of their values to changes in the underlying state variable, and the extent to which stock price movements are generated by information about new or expanded growth options. In addition, the well-known financial leverage effect would cause a decrease in the levered beta relative to the unlevered beta in case of good news.

3 Returns Data and Growth Opportunity Proxies

We collect monthly stock returns from CRSP, and annual financial statement data from the merged CRSP-Compustat database. Accounting data for fiscal years ending in calendar year t-1 are merged with monthly stock returns from July of year t to June of year t+1. Our selection criteria and construction of firm-specific variables, follow Fama and French (2001). The sample includes NYSE, AMEX, and NASDAQ shares with CRSP codes of 10 or 11, from June 1965 to June 2007. We exclude utilities, financial firms, and firms with book value of equity below K\$250 or assets below K\$500. We use a firm's market capitalization at the end of June of year t to calculate its book-to-market, leverage and earnings-to-price ratios, and dividend yield for that year.

As the weights of firms in growth options and assets in place are not observable, a common practice is to use proxy variables. A number of studies evaluate the performance of growth opportunity proxies. For example, Goyal, Lehn and Racic (2002), with a sample of U.S. defense industry firms, show that proxy variables track the changes in the industry's investment opportunities. Adam and Goyal (2007) also evaluate the performance of proxies for a firm's investment opportunity set. They show that, among commonly used proxies, market-to-book asset ratio has the highest information content with respect to investment opportunities and is least affected by other confounding factors. Any given proxy will potentially fail to measure the full extent of the investment opportunity set, and has its advantages and disadvantages. Erickson and Whited (2006) conclude that all the proxies for Tobin's q which they examine contain significant measurement errors. We therefore use several proxies motivated in the literature and again below, each with some qualities and limitations.

The first proxy for growth options which we use is the ratio of market-to-book value of assets (**Mba**). The book value of assets proxies for assets in place while the market value of assets proxies for the sum of assets in place and growth opportunities. So, the higher the Mba ratio is, the higher the proportion of growth options to firm value. As in Fama and French (2001), we define the market value of assets as book value of assets minus book value of equity plus market value of equity. Mba is similar to the reciprocal of the ratio of book value of assets to total firm value (A/V) used by Smith and Watts (1992). Smith and Watts note that the A/V ratio may have measurement problems for firms with long lived assets because assets are measured at historical cost less depreciation. This caveat applies to the Mba ratio. We also use other proxies.

The second proxy is the ratio of earnings-to-price (**Ep**), used for example by Kester (1984) and Smith and Watts (1992). We use the earnings available for common, i.e., the earnings before extraordinary items minus preferred dividends plus income statement deferred taxes if available. The larger the Ep ratio is, the larger the proportion of equity value attributable to earnings generated from assets in place rather than growth options. This is valid only for firms with non-negative earnings. When forming groups based on the Ep ratio, we put firms with negative earnings in a separate group. Ep and Mba ratios are growth measures very often used in the literature.

Our third proxy is the dividend yield (**Div**). Dividends are linked to investment through

the firm's cash flow identity. Jensen (1986) argues that firms with more growth options have lower free cash flows and pay lower dividends. It has been shown in some studies that growth firms tend to have lower dividend yields than non-growth firms. When sorting firms based on the dividend yield, we put zero-dividend firms in a separate group.

The final proxy for growth opportunities is the ratio of capital expenditures to net fixed assets (**Capex**). Capital expenditures are mostly seen as discretionary investment decisions. The higher the capital expenditures are, the greater the investment made by a firm to create new products, and therefore the greater the growth options. However, capital expenditures, a purely accounting measure, may be lumpy. Adam and Goyal (2007) suggest that Capex it may not be a very good proxy for investment opportunities by itself.

We also use the debt-to-equity ratio, (**Dtoe**). By Contracting theory, firms with significant growth options may have lower financial leverage because equity financing controls the potential under-investment problem associated with risky debt, see for example Myers (1977). Adam and Goyal (2007) show that proxy variables for growth options are affected by both investment opportunities and by financial constraint. Goyal, Lehn, and Racic (2002) show an inverse time-series relationship between debt levels of defense firms and their growth opportunities. Here, we track Dtoe mainly to infer changes in unlevered betas from changes in observed levered equity betas. Our results will allow us to derive unambiguous conclusion without resorting to specific levering formulas.

In summary, high growth opportunity firms are expected to have higher Mba and Capex ratios and lower Ep, Div, and Dtoe ratios. The literature generally documents positive but low correlations among different proxies, e.g., Adam and Goyal (2007). So using their joint use will not cause any multicollinearity. We obtain data items for these ratios from the merged CRSP-Compustat database. We update the proxies annually from 1965 to 2007 for each firm.

4 Empirical Results

4.1 Betas and financial leverage

At the end of every 3-year "ranking" period from July 1968-June 1971 to July 2001-June 2004, we assign firms to performance deciles on the basis of three-year cumulative returns. We denote pre- and post- ranking, the 3-year periods before and after the ranking period. Value-weighted monthly portfolio returns are formed for ranking and pre- and post-ranking periods. The pre-ranking periods start in July 1965-June 1968, and the post-ranking periods end in July 2004-June 2007. This methodology allows us to document the long-term behavior of the betas of winners and losers, in a manner robust to estimation error. To be included in the analysis, a firm needs thirty-six monthly returns and growth proxies for ranking as well as pre- and post-ranking periods. We exclude firms with share prices below \$1 at the end of any 3-year period to ensure that our results are not confounded by illiquid stocks. Unless mentioned otherwise, the statistics reported for a given group and period are time series averages of portfolio values over the sample. Analysis with medians produced similar results and are not reported.

Table 1 summarizes changes in systematic risk and financial leverage for losers and winners, confirming existing findings and showing some new results. We use the 30-day U.S. Treasury bill return as the risk-free rate and compute rolling betas annually, using three years of monthly portfolio excess returns over the ranking period, and the pre- and post- ranking periods. For each portfolio i, we estimate β over a given 3-year period with the usual market model regression

$$r_{it} - r_{ft} = a_i + \beta_{i,vw} (r_{mt} - r_{ft}) + \epsilon_{it}, \ t = 1, ..., 36,$$

where r_{it} is the monthly value weighted return on portfolio i, r_{ft} is the monthly risk-free rate, and r_{mt} is the monthly return on the the value weighted NYSE, AMEX and NASDAQ index. We also compute betas for the 4-factor model, with the regression

$$r_{it} - r_{ft} = \alpha_i + \beta_{i,mkt} r_{mkt,t} + \beta_{i,smb} r_{smb,t} + \beta_{i,hml} r_{hml,t} + \beta_{i,umd} r_{umd,t} + \epsilon_{it}, \quad t = 1, \dots, 36, \dots, 36, \dots, 10, \dots, 1$$

where r_{mkt} , r_{smb} , $r_{hml,t}$ and $r_{umd,t}$ are the returns on the market, size, book-to-market and momentum factors. The market factor mkt is the monthly return on the NYSE, AMEX and NASDAQ index in excess of the risk-free rate.

Panel A reports cumulative returns for each decile in the ranking and pre- and post-ranking periods, denoted periods 0, -1 and 1. The first three columns, "Ret. in %", show that the typical loser firm experiences a 53% cumulative loss over the 3-year ranking period, while the winner decile records a 264% return. Then, they both record similar returns, 48% for the loser and 40% for the winner, in the post-ranking period. Loser and winner deciles display some reversal as documented by DeBondt and Thaler (1985).

Consider now the average portfolio β_{vw} for each performance decile and period. The loser β_{vw} drops from 1.34 in the pre-ranking to 1.26 in the post-ranking period. In contrast, the winner β_{vw} increases from 1.20 to 1.27. Recall that we do not to use specific "unlevering" formulas to recover unlevered betas. The results reported here on levered betas and leverage always allow us to draw unambiguous inference about the direction of the changes in unlevered betas. Specific formulas would allow us to quantify the magnitude of the change, but this would of course limited to the formula used. Here, as their β_{vw} decreases, the Dtoe of the losers more than doubles from 25% in period -1 to 58% in period 1. The Dtoe of winners halves from 46% to 23%, as their β_{vw} actually increases. Clearly, the patterns of change in the betas of losers and winners contradict the predictions of the financial leverage hypothesis. Barring any changes in unlevered beta, an increase (decrease) in financial leverage would suggest an increase (decrease) in levered equity beta. The contradictory evidence reported here is consistent with large losses of growth options for the losers, implying a drop in their asset betas.

4.1.1 4-factor model betas

The results so far suggest that the operating leverage effect dominates the financial leverage effect. But if systematic risk is described by a multiple factor model as in Fama-French (1992),

 β_{vw} may give an incomplete description of the evolution of systematic risk for losers and winners. We repeat the analysis for the four factor betas. Namely, we report the changes in the four-factor model betas β_{mkt} , β_{smb} , β_{hml} and β_{umd} through pre- to post-ranking periods in Table 1, panel B.

Changes in β_{hml} are interesting since it is the sensitivity to the HML factor, which is the difference between returns on high and low book to market equity stocks. Firms with higher growth options should have lower HML beta. So, β_{hml} is useful in determining whether losers (winners) have indeed lost (gained) growth options. The book-to-market factor beta, β_{hml} is in table 1, panel B. It has an inverted U-shape pattern across performance groups in ranking period 0; both winners and losers have lower β_{hml} than average. To the extent that HML factor is inversely related to growth, this suggests that extreme performers are more growth oriented than the average firm. This is also true in the pre-ranking period. The pattern of changes in β_{hml} from pre- to postranking periods for extreme losers and winners is consistent with operating leverage. The typical loser firm's β_{hml} increases from -0.61 to -0.07. Losers do experience losses in growth opportunities and hence load relatively more on the HML factor over time. In contrast, the winner firms β_{hml} 's decrease from -0.23 to -0.58. Consistent with an increase in growth opportunities, their load on the HML factor decreases. From this evolution of β_{hml} , the losers appear to be firms with initially high growth potential which fail to realize this potential. The winners, are initially growth oriented firms which eventually capture the value presented by potential growth opportunities.

Unlike the book-to-market factor, the size factor SMB, the difference between returns on small and large firms, is not a clear growth proxy. Small, young firms may be more growth oriented, while losers that have lost growth options may also be smaller firms than average. Nevertheless, as the size factor SMB may proxy for other risks, disregarding it may bias the estimates of systematic risk. In the ranking period, the typical loser β_{smb} is 0.39 and the winner β_{smb} is 0.20, both larger than for the average firm. This U-shaped pattern is even more pronounced in the pre-ranking period. The changes from pre- to post-ranking periods are interesting. The typical loser β_{smb} increases from 0.25 to 0.56; over time losers become smaller as expected. The typical winner firm becomes larger on the other hand, as its β_{smb} decreases from 0.30 to 0.07. β_{smb} is far larger for the losers than for the winners in the post-ranking period, 0.56 vs. 0.07. In addition, the decrease in β_{smb} in the post-ranking period across performance deciles is almost monotonic. However, the post-ranking period β_{smb} is lower for the middle groups than for the extreme winners. This is consistent with the hypothesis that the winners include a number of small growth firms, in fact more small firms than the middle groups.

The momentum factor UMD is the return difference on recent winner and loser stocks. It is natural to expect losers to have heavy negative exposures to this factor during the ranking period. On the other hand, winners are expected to load positively on the momentum factor. The factor loadings on the momentum factor UMD are as expected. β_{umd} in the ranking period monotonically increases from -0.51 to 0.30 across performance decile portfolios. It seems that the momentum factor is doing a good job in catching the extreme performance during the ranking period. However, neither winner or losers, nor any other portfolio has a significant loading on the momentum factor in the pre- or post- ranking periods.

The results for the market beta β_{mkt} can be viewed as a robustness check of those for β_{vw} in panel A, to the extent that the four-factor model is more robust than the one-factor model. β_{mkt} is stable across period for each decile. β_{mkt} has a U-shaped distribution across the performance decile portfolios. Both winners and losers have larger market betas than the average firm. Due to the change in Debt equity ratio, as for β_{vw} in panel A, we conclude that the unlevered market beta of losers (winners) has decreased (increased).

The conclusion that firms suffer or gain proportionally higher losses or returns in growth options than in assets in place is robust to the measure of systematic risk used. Contradictory to the financial leverage hypothesis, as financial leverage increases (decreases) for losers (winners) over time, market beta at best remains constant or actually decreases (increases). The losers' (winners') increased (decreased) exposure to the HML factor over time is consistent with a proportionally higher loss (gain) in growth options. Finally, using a multi-factor model to measure systematic risk proves to be a more robust choice since the ranking period tends to be unrepresentative of the periods preceding or following it. For example, the cumulative returns of losers or winners in the pre- or post-ranking periods are nothing out of the ordinary unlike their returns in the rankingperiod. The Dtoe ratio in the ranking period over states the change in the financial leverage of extreme performers over time. For example, the financial leverage of losers go up over time, but not as much as the level suggested in the ranking period.

4.1.2 Robustness to extreme initial financial leverage

In the previous sections, we find a positive relationship between stock returns and unlevered betas, consistent with the "change-in-mix" effect in equation (3) dominating both the "moneyness" effect and the financial leverage effect. This is also consistent with the range of growth options in the middle region of figure 1. The natural question that follows is whether this result is robust to extreme initial financial leverage.

Financial leverage is likely to have the strongest effect on betas for the most highly levered firms as contracting theory implies that such firms have low growth options. Therefore, the financial leverage effect should be stronger for firms with a high initial leverage. Moreover, for these firms, the operating leverage effect can be weak, or might cause an inverse relationship between stock return and beta similar to the left region of figure 1. In essence, firms with very few growth options do not have much more to loose. Therefore, we might observe an inverse relationship between beta and returns for these firms.

To study changes in systematic risk among both high and low financial leverage firms, we repeat the analysis in Table 1 among Dtoe sub-samples. We first group stocks into three financial leverage (Dtoe) groups in period -1 (pre-ranking period) based on 30th and 70th percentile cutoff values. We then form period 0 (ranking period) cumulative return deciles within each leverage group. Value-weighted monthly returns are formed for ranking as well as pre- and post-ranking periods for these double-sort portfolios. We then essentially repeat the empirical analysis in the previous section. Table 2 reports the results.

Consider the first two rows in both panels of Table 2 which show the results on losers and winners formed among the low initial leverage sub-sample. Both the winner and loser portfolios are essentially composed of debt-free firms in period -1. The changes in loser and winner betas are very similar to the general case. The loser β_{vw} decreases from 1.48 in period -1 to 1.29 in period 1, and β_{mkt} decreases from 1.12 to 1.06. The increase in Dtoe from 3% to 27% allows us to conclude again that unlevered betas have decreased. In fact, the loser β_{hml} increases relatively over time from -0.95 to -0.39, suggesting a proportionally higher loss in growth options. On the other hand, there is essentially no change in winner β_{vw} , and β_{mkt} drops slightly from 1.04 to 0.96. The winner Dtoe undergoes a small increase from 5% to 7%, different from the large decrease seen in the Table 1. Given the changes in betas and financial leverage, unlevered betas may have slightly decreased, if at all. In terms of operating leverage, this is consistent with a firm in the right region of figure 1, where an increase in s, i.e., a decrease in operating leverage, causes a small change in β . It may also mean that for firms with an already high weight in growth options, positive news are unlikely to be related to a further increase in this weight. Namely, the condition (3) may not be met. The looser β_{hml} of -0.95 and the winner β_{hml} of -0.62 in period -1 suggest that these low leverage firms have high initial growth options.

We now turn to losers and winners in the high initial leverage group, with Dtoe of 117% and 141%, respectively. For the winners, both β_{vw} and β_{mkt} essentially remain constant over time. Given the large reduction in Dtoe, from 141% to 53%, the winners' unlevered betas must have increased. The same conclusion follows from the relative decrease in β_{hml} over time from 0.17 to -0.08. Their terminal β_{hml} of -0.08 corresponds to a period 1 value between groups 7 or 8, well into the middle of the distribution in growth opportunity. These may be firms with very good news on the weight in growth options, condition (3). It is not surprising then that, as average winners, they exhibit a positive relationship between returns and unlevered betas.

We can see that even the losers with high initial financial leverage exhibit a positive operating leverage effect. Their β_{vw} decreases from 1.34 to 1.23, and β_{mkt} decreases from 1.22 to 1.17. On the other hand, their financial leverage increases from 117% in period -1 to 147% in period 1. With an increasing financial leverage, the decrease in levered β implies a decrease in unlevered beta, hence a decrease in growth options. The large increase in β_{hml} from 0.07 to 0.43 confirms this. In summary, even firms with initially few growth options, which then suffer a further reduction of their value, still exhibit a positive operating leverage effect. This would put them on the central region of the top plot of Figure 1, although one could have assumed that, initially already in the left region and moving further left, they would have displayed a negative relation between beta and returns.

The two middle rows of both panels in Table 2 report on the average leverage group. Again, the increase in leverage, from 25% to 60% for the losers, joint with the decrease in β_{vw} from 1.34 to 1.24 suggest that, as the general population of losers, their unlevered betas decrease. This conclusion is also supported by the large increase in β_{hml} from -0.42 to 0.18. The winners experience a slight decrease in leverage from 28% to 23%. The patterns of change in β_{vw} , β_{mkt} and β_{hml} all suggest that their unlevered betas increase.

4.2 Betas and growth options

The results so far are consistent with the hypotheses that growth options have higher betas and are more volatile than assets in place. We now concentrate on the first hypothesis. While the previous analysis was akin to a time series study of changes in growth opportunities, we now document the cross-sectional link between betas and firm characteristics argued in section 3 to proxy for growth options. This will also help gauge the quality of these variables as proxies of growth options.

At the end of every June from 1968 to 2004, firms are allocated to increasing growth opportunity groups on the basis of increasing ratios of capital expenditures to fixed assets (Capex) and market to book value of assets (Mba), and decreasing dividend yield (Div) and ratios of earnings to price (Ep) and debt to equity (Dtoe). Firms are allocated to 10 groups based on Capex and Mba, and 11 groups based on Div, Ep and Dtoe. Firms with zero dividends and debt, and non-positive earnings are grouped into portfolio 11. Table 3 reports aggregate growth opportunity proxy values, betas with respect to the value weighted NYSE, AMEX and NASDAQ market index (β_{vw}) and the four-factor model risk estimates (β_{mkt} , β_{hml} , β_{smb} and β_{umd}), and aggregate debt to equity ratios (Dtoe in %) across low-to-high growth opportunity portfolios. The numbers reported are time-series averages of portfolio values over thirty-seven overlapping 3-year post-ranking periods from July 1968-June 1971 to July 2004-June 2007. Panel A reports results on Capex based growth deciles. The grouping highlights the crosssectional variability in Capex, 11.74% to 36.25%, from decile 1 to 10. Remember that individual firms are allocated to portfolios based on ranking period values, and the numbers reported in Table 3 are post-ranking values. The monotonic increase of Capex from decile 1 to 10 highlights the fact that growth proxies tend to be persistent over time. Deciles 1 and 10 have levered β_{vw} 's of 1.11 and 1.44. Given their Dtoe's of 61.75% and 17.87%, this means that the unlevered beta of low Capex stocks is even lower than that of high Capex stocks. Similar conclusions follow from β_{mkt} . Although the relation is U-shaped, higher growth deciles tend to have larger beta's than lower growth ones. The book-to-market risk factor β_{hml} , argued to be inversely related to growth options, is indeed here inversely related to Capex. The size factor β_{smb} has a U-shaped relationship with Capex. This is consistent with the fact that both low and high growth opportunity groups may include small firms. There is no discernible relationship between Capex ranking and momentum risk factor beta, β_{umd} .

Panel B, which reports results based on Mba sorts, leads to similar conclusions. However, the conclusions that follow from either β_{vw} or β_{mkt} are not as strong as those in panel A. Naturally, there is a monotonic negative relationship between Mba and β_{hml} . The size factor β_{smb} and Dtoe are also negatively related to Mba, suggesting that low Mba groups tend to contain smaller stocks than high Mba ones.

Panels C and D report results on dividend yield (Div) and earning to price ratio (Ep) based sorts. Both of these panels lead to similar conclusions as the previous two albeit with differences due to the nature of their high growth decile 11. Decile 11 contains firms with zero dividends and non positive earnings in the ranking period. Deciles 10 (rows marked with *High*) in either panel tend to have higher β_{vw} and β_{mkt} , and lower Dtoe than deciles 1. These relationships are nearly monotonic across deciles 1 through 10. Both proxies display an unambiguous positive relationship between proxy and beta and an inverse relationship between proxy and financial leverage. Therefore, unlevered betas must also have a positive relationship with the growth opportunity proxies. The conclusion is robust to any reasonable relationship between levered and unlevered betas, only requiring levered beta to increase with financial leverage for a given unlevered beta. We can even infer that the positive relationship relationship between growth options and unlevered betas is stronger than that reported with equity betas. The book-to-market risk factor β_{hml} is inversely related to both proxies, supporting the view that unlevered betas have a positive relationship with the growth opportunity proxies.

Zero-dividend firms (row labeled Div=0) in panel C have the highest equity betas but not the lowest Dtoe. Their Dtoe of 40.26% places them somewhere between deciles 3 and 4, whereas their β_{hml} of -0.52 places them between deciles 9 and 10. While many zero-dividend firms are indeed growth firms, a number may just be distressed firms. The same observation can be made for non-negative earnings firms in panel D (row labeled $Ep \leq 0$). While lower Ep ratios can be argued to be related to higher growth options, it is hard to extend the reasoning to negative earnings. Indeed both β_{hml} of 0.11 and Dtoe 74.20% indicate that these firms may have few growth options. Their β_{hml} places them somewhere between deciles 4 and 5, and Dtoe places them between deciles 1 and 2.

Even though we do not consider Dtoe as a growth proxy per se, we nevertheless include it in Table 3. Panel E repeats the same analysis of this section on Dtoe sorted portfolios. The results suggest that high Dtoe firms tend to have high betas. Especially, the near monotonic decrease in β_{mkt} from high to low Dtoe show that the implications of the financial leverage hypothesis hold when growth options have been accounted for by the HML factor. Not surprisingly, high Dtoe firms tend be small and low Dtoe firms tend to be large as suggested by β_{smb} . Once again, the zero debt firms (decile 11) prove to be different than the rest. Their β_{smb} of 0.29 places them between decile 1 and 2, suggesting that *zero-debt* firms are actually very small and quite different than *low debt* firms.

The relations observed in Table 3 between growth proxies and, indirectly, unlevered betas are consistent with the hypothesis that higher growth options result in higher betas. Or, considering this hypothesis pretty uncontroversial, the results demonstrate the quality of these observables as proxies for growth options. As the firms are grouped in the ranking-period and systematic risk is measured in the post-ranking period in our analysis, the cross-sectional relationship between betas and proxies may have some predictive power on betas. We return to this later.

4.3 Cross-sectional variation in systematic risk

The above analysis examines the relationship between betas and proxies one at a time. We now examine the joint ability of the growth opportunity proxies to explain cross-sectional variations in asset betas. To do this, we estimate the following regression:

$$\beta_{i,t+1} = \delta_t X_{i,t} + \gamma_t \Delta X_{i,t} + \epsilon_{i,t+1} \quad i = 1 \dots 50,$$
(5)

where X is the vector of proxies (Mba, Capex, Div, Ep, Dtoe) measured at t and ΔX is the change in X from t to t + 1. The rational for including proxy differences is to check if, on average, recent changes in proxies have marginal explanatory power over the *long-run* values of the proxies.

We form 50 portfolios to reduce measurement errors in beta estimates. In each of the thirtyseven overlapping 3-year periods covering July 1965-June 1968 to July 2001-June 2004, firms are allocated to 50 portfolios on the basis of cumulative returns. Aggregate portfolio growth proxies for this ranking period and the following 3-year post-ranking period (July 1968-June 1971 to July 2004-June 2007) are calculated at the end of each 3-year period. Portfolio systematic risk factor loadings are estimated using thirty-six monthly value weighted portfolio returns over the postranking period. In the above regression, the dependent variables are estimates of post-ranking period systematic risk and the independent variables are lagged (ranking period, denoted by t) proxies and changes (Δ) in the level of proxies from ranking to post-ranking period.

We run (5) as thirty-seven overlapping cross-sectional regressions. To facilitate an economic interpretation of δ and γ , we standardize the proxies by their cross-sectional mean and variance, recomputed periodically. That is, δ is the change in β for a one cross-sectional standard deviation change in the proxy. This standardization may also be preferable if proxies exhibit strong time trends or changes through the sample period.

Table 4, panel A reports results for the dependent variables β_{vw} and β_{mkt} . Subscripts (-1)

refer to the estimates of δ in (5). The column "mean" shows the average of the 37 estimates. Q_1 and Q_3 are the first and third quartiles of the distribution of the 37 estimates. "#" shows the number of estimates with the expected sign. Next to it is the the Newey-West corrected t-statistics accounting for three lags of autocorrelation. \bar{R}^2 and \bar{R}^2_{-1} report on the adjusted R-squares of the regressions, with all the independent variables and that with only the lagged (-1) variables.

The first clear result, by inspection of the R-squares is that the fit is very high. The proxies explain a large fraction of the cross-section of systematic risk. Inspection of the R-squares produces two clear results. For β_{vw} , the R-square averages 59%, with three quarters above 52%. For β_{mkt} , the average R-square is lower. Second, the lagged values of the proxies, not their recent changes are at the source of this explanatory power. This is seen clearly by comparing the R-squares of the full regression in (5) with \bar{R}^2_{-1} reported below (the R-square of a regression without ΔX). The coefficient estimates for the change variables ΔX confirm this result. They are mostly insignificant, and about half the time of the correct sign, as expected under the null hypothesis. The only possible exception is ΔDiv , with the expected sign most of the time and a significant t-statistic. The validity of each proxy individually can also be verified. We expect positive coefficients for Capex and Mba. negative for Div and Ep. Capital expenditures and dividends are significant and with the correct sign about every single period. The coefficient of $Dtoe_{-1}$ is significant and with the correct sign two-thirds of the time. This shows that one can recover the sign expected by the financial leverage hypothesis, once growth proxies have been accounted for. We note only two exceptions. Both for β_{vw} and β_{vw} , the slope estimate for Mba₋₁ is contradictory to what we would expect. The coefficient of Ep_{-1} for β_{vw} has a similar pattern.

As our 50 portfolios contain fewer stocks than the standard 20 or 40 portfolios used in a typical empirical study, the measurement errors in their betas are consequently larger. However, measurement errors on a left-hand side variable do not induce a bias, they only lower the fit of (5). One goal of the regression in (5) is to precisely assess to what extent we can filter out estimation error through the use of growth opportunity proxies. In order to see the impact of having more or less than 50 portfolios in the cross-section, we re-run the regression in (5) with 25 and 100 portfolios. Panel B summarizes average fit statistics for the dependent variables in panel A as

well as book-to-market (β_{hml}) , size (β_{smb}) and momentum (β_{umd}) factor loadings for 25, 50 and 100 portfolio cross-sections. As expected, having fewer portfolios in the cross-section, and thereby including more stocks in each portfolio, dramatically increases the fit.

To summarize, the lagged growth opportunity proxies explain up to two thirds of crosssectional differences in systematic risk. The relationship between betas and each proxy most often has the desired sign given that growth options have higher betas. Recent changes in the proxies do not have marginal explanatory power over and above the lagged values of the proxies, which is consistent with a slow variation of true betas.

4.4 Return predictability and changes in growth options

Table 1 showed that loser betas decline and winner betas increase. These patterns, which arise because of losses (or gains) in growth options, could induce predictability in extreme portfolio returns if investors are slow to account for the implication of growth options on betas. Consider the following three-period scenario for a loser stock. In period one, the stock incurs negative returns. If investors anchor their beliefs on large negative stock return and the financial leverage effect but ignore potential losses in growth options, they might believe that the equity beta is higher than it really is. Assume that the market excess return is positive in period 2. If investors have not yet accounted for the loser's decreased growth options, the loser stock rises according to the "older" beta that is too high. In period 3, investors adjust to the new, lower beta, correcting for the excessive rise of period 2. If this is the case, we expect to see a negative relationship between the excess return in period 2. For winners, a similar reasoning could produce a positive relationship between the winner and the lagged market returns.

To examine this, we analyze the relationship between extreme portfolio excess returns and the previous year market excess returns. At the end of June of year t, firms are allocated to decile portfolios on the basis of past 3-year cumulative returns. Value weighted returns are tracked for 12 months over the second year after portfolio formation, resulting in a series of monthly portfolio returns covering July t+1 to June t+2. This process is repeated every year from 1968 to 2005, providing a series of 456 monthly returns from July 1969 to June 2007. Using this second-year monthly return series, annual rolling portfolio excess returns are calculated and related to the contemporaneous and lagged market excess returns:

$$r_{p,t} = \alpha_{0,p} + \beta_p \ r_{m,t} + \beta_{p,-1} \ r_{m,t-1} + \epsilon_{p,t},$$

Table 5 shows the results of this regression using 445 overlapping annual observations. The estimate of $\beta_{p,-1}$ increases monotonically from losers to winners, with the exception of the one on the highest past-performing portfolio. For the losers, the estimate of $\beta_{p,-1}$ is -0.425 with a t-statistic of -4.63. For the winners, the estimate has the correct sign but is insignificant. However, the estimate of $\beta_{p,-1}$ for decile 9 (the second highest past-performing portfolio) is a highly significant 0.099. These results show that there is some evidence consistent with a scenario in which it takes more than a year for the market to fully incorporate changes in betas for both the losers and the winners.

5 Conclusions

The empirical literatures still makes much more case of the financial than the operating leverage effect. This is somewhat surprising given that the predictions of the financial leverage effect are somewhat at odds with the evidence. In particular, as we emphasize in this paper, betas of stocks that have experienced very high returns do not decline as the financial leverage suggests, and betas of stocks that have experienced negative returns decline significantly, which is again inconsistent with the theory.⁷ Moreover, the equity betas of financially distressed firms seem to decline as their financial condition deteriorates even though the unsystematic risk and total risk increase.⁸ While this evidence is inconsistent with the Hamada and Rubinstein leverage

⁷Contradictions with the predictions of financial leverage are also reported in the empirical corporate finance literature. Firms that take actions that increase financial leverage do not experience increases in their market betas. See for example Healy and Palepu (1990), Bartov (1991), and Dann, Masulis, and Mayers (1991), Denis and Kadlec (1994), or Kaplan and Stein (1990).

⁸See, for example, Aharony, Jones, and Swary (1980) and Altman and Brenner (1981). They attribute the decline in betas to possible decreases in the systematic risk of earnings, but do not explain why this may be the case.

adjustments, it is consistent with the hypothesis that firms increase (decrease) leverage when the value of their growth options decline (increase).

Several recent papers have linked growth opportunities to systematic risk. For instance, Berk, Green and Naik (1999), Anderson and Garcia-Feijoo (2002) and Carlson, Fisher and Giammarino (2003) show that the exercise of growth options change a firm's systematic risk. Cao, Simin and Zhao (2007) argue that a significant portion of the upward trend in *idiosyncratic* risk can be explained by changes in the level and variance of growth options, as well as the capital structure of firms - subsiding the profitability based explanations in the literature. Recent general equilibrium models link the evolution of betas to latent state variables that include measures of growth options. These structural models of betas are however difficult to implement. Our cross-sectional regressions can be justified as a practical and simple reduced form for these models.

Using Myers' (1977) description of the firm as a combination of assets in place and growth opportunities, we are able to analyze the effects of changes both in the financial leverage and the asset structure of firms on market betas. Our results suggest that the inconsistency between the financial leverage change and the change in systematic risk can at least partially be explained by the relation between past stock returns and changes in a firm's mix between growth options, which generally have high betas, and assets in place, which generally have low betas. A dramatic decline in stock prices causes a proportionally larger reduction in the value of growth opportunities relative to the value of assets in place. Even though financial leverage increases, the reduction in the asset beta dominates and the systematic risk of losers decline. Similarly, there is an increase in the systematic risk of winner firms, in contrast to the predictions of the financial leverage effect.

We explore whether evidence of the financial leverage effect will be stronger for the stocks of highly levered firms that subsequently experience very negative returns. The high leverage of these firms should increase the importance of the leverage effect, and since these firms tend to have very few growth options, the offsetting effect should be minimized. However, we find that even for these firms, the betas of past losers tend to decrease.

Finally, we consider the possibility that investors fail to appreciate these beta changes,

which would imply that past winners and losers would either over or underreact to market moves. We present preliminary results that suggest that the losers tend to have betas that are too high, implying that they overreact to market returns. This finding will be the subject of future research. APPENDIX: Partial derivative of $\eta_G = \frac{\beta_G}{\beta_S}$ with respect to the moneyness ratio.

Consider $N(d_1), N(d_2), r_f, T$ as in the standard Black-Scholes notation. Denote S the underlying value, C the strike price, and m = S/C the moneyness ratio. The elasticity of the option G with respect to the underlying S is

$$\eta_G = \frac{SN(d_1)}{G} = \frac{SN(d_1)}{SN(d_1) - Ce^{-r_f T}N(d_2)} = \left[1 - \frac{1}{m}e^{-r_f T}\frac{N(d_2)}{N(d_1)}\right]^{-1} \ge 1.$$

The partial derivative of η_G with respect to the moneyness ratio m is

$$\frac{\partial \eta_G}{\partial m} = e^{-r_f T} \eta_S^2 \frac{\partial \left(\frac{N(d_2)}{mN(d_1)}\right)}{\partial m} \\
= e^{-r_f T} \eta_S^2 \left[-\frac{N(d_2)}{m^2 N(d_1)} + \frac{1}{mN^2(d_1)} (N(d_1)Z(d_2)\frac{\partial d_2}{\partial m} - N(d_2)Z(d_1)\frac{\partial d_1}{\partial m}) \right]$$
(6)

where $Z(\cdot)$ is the standard normal density function, $d_1 = \frac{ln(m) + (r_f + 0.5\sigma^2)T}{\sigma\sqrt{T}}$, and $d_2 = d_1 - \sigma\sqrt{T}$.

Note that $\frac{\partial d_1}{\partial m} = \frac{\partial d_2}{\partial m} = \frac{1}{m\sigma\sqrt{T}}$, recall that $\eta_G = SN(d_1)/G$, and replace m with $\frac{S}{C}$. Equation (6) simplifies as

$$\frac{\partial \eta_G}{\partial m} = -\frac{C^2 e^{-r_f T}}{S^2 \sigma \sqrt{T}} N(d_2) N(d_1) \left(\sigma \sqrt{T} - \frac{Z(d_2)}{N(d_2)} + \frac{Z(d_1)}{N(d_1)}\right).$$

Galai and Masulis (1976, p. 76-77) show that $\sigma\sqrt{T} > \frac{Z(d_2)}{N(d_2)} - \frac{Z(d_1)}{N(d_1)}$. Hence, $\frac{\partial \eta_G}{\partial m}$ is negative.

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Table 1: Portfolio characteristics based on cumulative returns in the ranking period Firms are allocated to deciles ranked by cumulative returns over thirty-four overlapping 3-year periods covering July 1968-June 1971 to July 2001-June 2004. The column headers 0, -1, and 1, refer to the ranking period, and the two 3-year periods preceding (July 1965-June 1968 to July 1998-June 2001) and following (July 1971-June 1974 to July 2004-June 2007) the ranking period. Value-weighted monthly portfolio returns are formed for ranking as well as pre- and post-ranking periods. Panel A reports cumulative returns (Ret. in %), betas with respect to the value weighted NYSE, AMEX and NASDAQ market index (β_{vw}) and aggregate debt to equity ratios (Dtoe in %) for decile portfolios. Panel B shows the four-factor model risk factor loadings (β_{mkt} , β_{hml} , β_{smb} and β_{umd}). The numbers reported are time-series averages of portfolio values.

Group	R	et. in	%		Dt	Dtoe in $\%$				
Return	-1	0	1	-1	0	1	-1	0	1	
Loser	75	-53	48	1.35	1.34	1.26	25	82	58	
2	58	-28	48	1.21	1.17	1.12	28	60	45	
3	53	-10	52	1.07	1.07	1.01	27	51	43	
4	40	7	47	1.03	0.98	0.95	36	48	45	
5	41	23	48	0.99	0.91	0.93	38	47	43	
6	47	40	47	0.96	0.95	0.95	37	37	36	
7	39	61	45	0.96	0.93	0.95	36	32	34	
8	38	89	45	0.98	0.96	0.99	43	29	30	
9	41	134	49	1.04	1.04	1.07	42	24	28	
Winner	40	264	40	1.21	1.20	1.27	46	16	23	

Panel A: Returns, CAPM betas and leverage

Panel B: 4-factor	model	parameter	estimates
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Group		β_{MKT}			β_{HML}			β_{SMB}			β_{UMD}	
Return	-1	0	1	-1	0	1	-1	0	1	-1	0	1
Loser	1.12	1.17	1.13	-0.61	-0.26	-0.07	0.25	0.39	0.56	-0.02	-0.51	-0.22
2	1.06	1.10	1.11	-0.34	-0.15	0.04	0.10	0.22	0.30	-0.01	-0.29	-0.05
3	1.01	1.06	1.05	-0.18	-0.05	0.06	0.06	0.11	0.09	-0.02	-0.25	-0.12
4	1.02	0.99	1.00	-0.12	0.01	0.17	-0.05	0.03	0.01	-0.03	-0.25	-0.11
5	0.99	0.94	0.99	-0.06	0.07	0.17	-0.06	-0.02	-0.04	-0.05	-0.15	-0.09
6	1.00	0.96	0.98	-0.01	0.02	0.07	-0.03	-0.12	-0.11	-0.04	-0.04	-0.03
7	0.99	0.94	0.96	-0.01	0.04	-0.01	-0.07	-0.05	-0.12	-0.02	0.03	-0.03
8	0.98	0.99	0.97	-0.04	0.07	-0.11	-0.02	-0.09	-0.10	-0.06	0.09	0.00
9	1.02	1.01	0.97	-0.10	-0.07	-0.29	0.10	-0.01	-0.07	-0.06	0.15	0.03
Winner	1.07	1.02	1.04	-0.23	-0.42	-0.58	0.30	0.20	0.07	-0.02	0.30	0.04

Table 2: Portfolio characteristics based on a double sort: Financial leverage sorts in the pre-ranking period and cumulative return sorts in the ranking period

Firms are first allocated into three financial leverage (Dtoe) groups in the pre-ranking period -1 based on 30th and 70th percentile cutoff values. Then, within each leverage group, firms are grouped into cumulative return deciles in the ranking period 0. Please see Table 1 for the definition of ranking, and pre- and post-ranking periods. Panel A reports cumulative returns (Ret. in %), betas with respect to the value weighted NYSE, AMEX and NASDAQ market index (β_{vw}) and aggregate debt to equity ratios (Dtoe in %) for double sort portfolios. Panel B shows the four-factor model risk factor loadings (β_{mkt} , β_{hml} , β_{smb} and β_{umd}). The numbers reported are time-series averages of portfolio values.

Gr	oup	Re	et. in 9	70		β_{VW}		D	toe in	%	
Dtoe	Return	-1	0	1	-1	0	1	-1	0	1	
Low	Loser	143	-57	47	1.48	1.49	1.29	3	26	27	
Low	Winner	80	259	45	1.26	1.24	1.28	5	4	7	
Middle	Loser	51	-49	60	1.34	1.25	1.27	25	84	60	
Middle	Winner	35	240	37	1.15	1.19	1.23	28	16	23	
High	Loser	19	-47	52	1.34	1.28	1.23	117	253	147	
High	Winner	10	304	42	1.23	1.21	1.27	141	39	53	

Panel A: Returns, CAPM betas and leverage

			-											
Gr	oup		β_{MKT}			β_{HML}			β_{SMB}			β_{UMD}		
Dtoe	Return	-1	0	1	-1	0	1	-1	0	1	-1	0	1	
Low	Loser	1.12	1.22	1.06	-0.95	-0.59	-0.39	0.38	0.30	0.55	0.05	-0.55	-0.21	
Low	Winner	1.04	0.98	0.96	-0.62	-0.71	-0.88	0.24	0.13	-0.01	0.02	0.27	-0.02	
Middle	Loser	1.15	1.15	1.21	-0.42	-0.05	0.18	0.25	0.44	0.59	-0.05	-0.48	-0.12	
Middle	Winner	1.06	1.06	1.07	-0.16	-0.25	-0.48	0.31	0.15	0.07	-0.07	0.29	0.07	
High	Loser	1.22	1.22	1.17	0.07	0.44	0.43	0.55	0.86	0.85	-0.19	-0.41	-0.21	
High	Winner	1.13	1.10	1.14	0.17	0.10	-0.08	0.69	0.51	0.40	-0.12	0.22	0.09	

Table 3: Systematic risk characteristics versus growth proxies

At the end of every June from 1968 to 2004, firms are allocated to increasing growth opportunity groups on the basis of increasing ratios of capital expenditures to fixed assets (Capex) and market to book value of assets (Mba), and decreasing dividend yield (Div) and ratios of earnings to price (Ep) and debt to equity (Dtoe). Firms are allocated to 10 groups based on Capex and Mba, and 11 groups based on Div, Ep and Dtoe. Firms with zero dividends and debt, and non-positive earnings are grouped into portfolio 11. This table reports aggregate growth opportunity proxy values, betas with respect to the value weighted NYSE, AMEX and NASDAQ market index (β_{VW}) and the fourfactor model risk factors (β_{MKT} , β_{HML} , β_{SMB} and β_{UMD}), and aggregate debt to equity ratios (Dtoe in %) across low-to-high growth opportunity portfolios over thirty-seven overlapping 3-year post-ranking periods from July 1968-June 1971 to July 2004-June 2007. Growth opportunity proxies and debt to equity ratios are measured at the end of a given 3-year period. The numbers reported are time-series averages of portfolio values.

Panel A: Growth proxy is increasing in percent Capex

		r,	,		- F		
Growth	Capex	β_{VW}	β_{MKT}	β_{HML}	β_{SMB}	β_{UMD}	Dtoe
Low	11.74	1.11	1.09	0.27	0.37	0.01	61.75
2	14.41	0.92	0.94	0.18	0.01	-0.02	44.77
3	16.09	0.87	0.93	0.15	-0.07	0.01	40.77
4	17.74	0.93	1.01	0.08	-0.16	0.02	33.44
5	19.38	0.92	0.97	-0.02	-0.19	-0.04	31.56
6	21.20	0.96	0.99	-0.09	-0.13	-0.01	31.52
7	23.80	1.09	1.03	-0.25	-0.11	-0.01	30.49
8	25.17	1.12	1.02	-0.31	0.00	-0.08	32.57
9	28.51	1.24	1.03	-0.52	0.08	-0.08	23.83
High	36.25	1.44	1.13	-0.73	0.27	-0.09	17.87

Panel B: Growth proxy is increasing in percent Mba

Growth	Mba	β_{VW}	β_{MKT}	β_{HML}	β_{SMB}	β_{UMD}	Dtoe
Low	91.77	1.05	1.08	0.53	0.41	-0.05	71.94
2	101.57	1.06	1.11	0.52	0.24	-0.10	87.20
3	105.86	0.99	1.09	0.51	0.08	-0.09	88.80
4	118.80	1.00	1.06	0.34	0.04	-0.02	58.63
5	129.92	0.95	1.02	0.21	-0.02	0.00	48.22
6	141.10	1.00	1.03	0.08	-0.08	-0.01	39.24
7	157.88	1.02	1.01	-0.01	-0.05	0.00	33.38
8	181.95	1.02	0.99	-0.15	-0.06	-0.04	22.16
9	233.19	1.01	0.95	-0.36	-0.09	-0.02	13.47
High	364.59	1.09	0.93	-0.70	-0.11	-0.02	5.98

Panel C: Growth proxy is decreasing in percent Div										
Growth	Div	β_{VW}	β_{MKT}	β_{HML}	β_{SMB}	β_{UMD}	Dtoe			
Low	4.94	0.80	0.94	0.56	-0.09	-0.07	64.59			
2	4.19	0.84	0.97	0.34	-0.17	-0.05	55.98			
3	3.71	0.88	0.99	0.22	-0.16	-0.07	47.70			
4	3.22	0.88	0.96	0.11	-0.16	-0.04	34.62			
5	2.96	0.92	0.97	0.03	-0.14	-0.03	33.43			
6	2.52	0.93	0.96	-0.05	-0.12	-0.01	28.32			
7	2.22	0.98	0.95	-0.23	-0.12	-0.02	23.86			
8	1.72	1.01	0.96	-0.31	-0.06	-0.03	21.53			
9	1.33	1.09	1.03	-0.37	0.03	-0.01	22.24			
High	0.68	1.20	1.05	-0.54	0.07	-0.03	16.25			
Div = 0	0.31	1.50	1.18	-0.52	0.47	-0.03	40.26			

 Table 3: Systematic risk characteristics versus growth proxies - continued

Panel D: Growth proxy is decreasing in percent Ep

				-	-	-	
Growth	Ep	β_{VW}	β_{MKT}	β_{HML}	β_{SMB}	β_{UMD}	Dtoe
Low	7.59	1.07	1.15	0.56	0.23	-0.11	101.60
2	8.34	0.96	1.03	0.33	0.04	-0.06	62.34
3	8.48	0.92	0.99	0.24	-0.04	-0.05	48.01
4	8.03	0.93	0.98	0.16	-0.06	-0.04	37.04
5	8.09	0.94	0.96	0.07	-0.14	-0.02	39.69
6	7.12	0.98	0.96	-0.05	-0.09	-0.04	27.93
7	6.52	0.97	0.94	-0.21	-0.11	0.01	25.64
8	5.80	1.01	0.95	-0.30	-0.11	-0.02	19.47
9	4.83	1.07	0.96	-0.48	-0.01	-0.03	18.08
High	3.57	1.27	1.11	-0.56	0.08	0.01	18.74
$Ep \leq 0$	4.91	1.35	1.18	0.11	0.56	-0.07	74.20

Panel E:	Growth	proxv	is	decreasing	in	percent	Dtoe
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Growth	Dtoe	β_{VW}	β_{MKT}	β_{HML}	β_{SMB}	β_{UMD}
Low	182.63	1.19	1.21	0.56	0.44	-0.10
2	95.17	1.06	1.10	0.33	0.17	-0.05
3	66.52	0.93	1.00	0.34	0.09	-0.05
4	51.34	0.99	1.04	0.24	0.00	-0.04
5	38.68	1.02	1.06	0.17	-0.04	0.01
6	29.15	0.97	1.02	0.10	-0.12	-0.02
7	24.52	0.97	0.98	-0.07	-0.16	-0.01
8	15.81	0.96	0.93	-0.28	-0.17	-0.02
9	8.68	1.03	0.93	-0.44	-0.12	0.00
High	4.04	1.16	0.96	-0.67	-0.04	-0.06
Dtoe = 0	2.75	1.20	0.99	-0.49	0.29	0.03

Table 4: Cross-sectional variation in systematic risk

This table reports the results of cross-sectional regressions of systematic risk factor loadings on growth opportunity proxies. The proxies used are the ratio of capital expenditures to fixed assets (Capex), market to book value of assets (Mba), dividend yield (Div), the ratio of earnings to price (Ep) and debt to equity (Dtoe) ratio. In each of the thirty-seven overlapping 3-year periods covering July 1965-June 1968 to July 2001-June 2004, firms are allocated to 50 portfolios on the basis of cumulative returns. Aggregate portfolio growth proxies for this ranking period and the following 3-year post-ranking period (July 1968-June 1971 to July 2004-June 2007) are calculated at the end of each 3-year period. Portfolio systematic risk factor loadings are calculated using thirty-six monthly value weighted portfolio returns over the post-ranking period. In Panel A, the dependent variables are post-ranking period market beta with respect to the value weighted NYSE, AMEX and NASDAQ index (β_{VW}) and the market beta from the 4-factor model (β_{MKT}) . The independent variables are lagged (ranking period, denoted by $_{-1}$) proxies and changes (Δ) in the level of proxies from ranking to post-ranking period. For each of the thirty-seven cross-sectional regressions, the independent variables are standardized across the 50 observations. In Panel A, we report the time-series average, the first and third quartile values of parameter estimates, the Newey-West corrected t-statistics accounting for three lags of autocorrelation, average fit statistics and the number of estimates with the expected sign, #. \bar{R}^2 and \bar{R}^2_{-1} report on the adjusted R-squares of the regressions, with all the independent variables and that with only the lagged (-1) variables. Panel B reports average fit statistics for the dependent variables in Panel A as well as book-to-market (β_{HML}), size (β_{SMB}) and momentum (β_{UMD}) factor loadings for 25, 50 and 100 portfolio cross-sections.

Panel A:	Dependent	variables,	β_{VW}	and	β_{MKT}
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			β_{VW}					β_{MKT}		
	Mean	Q_1	Q_3	#	\mathbf{t}	Mean	Q_1	Q_3	#	\mathbf{t}
Intercept	1.116	1.082	1.149	37	57.16	 1.054	1.018	1.079	37	85.59
$Capex_{-1}$	0.047	0.005	0.097	28	3.04	0.011	-0.027	0.049	23	1.03
Div_{-1}	-0.189	-0.256	-0.146	36	-15.56	-0.099	-0.148	-0.056	33	-7.41
Mba_{-1}	-0.098	-0.133	0.004	11	-2.50	-0.118	-0.178	-0.010	9	-3.46
Ep_{-1}	-0.018	-0.034	0.069	17	-0.44	0.013	-0.013	0.074	12	0.49
$Dtoe_{-1}$	0.026	-0.019	0.073	23	1.46	0.024	-0.040	0.089	23	1.12
$\Delta Capex$	0.009	-0.032	0.046	24	0.87	0.001	-0.034	0.017	20	0.08
ΔDiv	-0.096	-0.126	-0.055	34	-8.35	-0.063	-0.093	-0.029	32	-6.78
ΔMba	-0.094	-0.153	0.009	12	-2.53	-0.102	-0.145	-0.029	8	-3.16
ΔEp	0.000	-0.020	0.055	11	0.01	0.000	-0.019	0.059	15	-0.01
$\Delta Dtoe$	-0.008	-0.058	0.050	20	-0.47	0.000	-0.038	0.053	21	0.03
\bar{R}^2	0.594	0.521	0.678			0.309	0.192	0.429		
\bar{R}^{2}_{-1}	0.498	0.404	0.581			0.233	0.135	0.343		

Panel B: Average fit

	R^2					R^{2}_{-1}				
	Dependent variables					 Dependent variables				
Portfolio	β_{VW}	β_{MKT}	β_{HML}	β_{SMB}	β_{UMD}	β_{VW}	β_{MKT}	β_{HML}	β_{SMB}	β_{UMD}
25	0.722	0.435	0.698	0.673	0.368	0.608	0.329	0.629	0.566	0.228
50	0.594	0.309	0.589	0.567	0.279	0.498	0.233	0.534	0.459	0.168
100	0.461	0.194	0.477	0.444	0.206	0.371	0.130	0.410	0.339	0.111

Table 5: Predictability in Loser and Winner portfolio returns

At the end of June t, firms are allocated to decile portfolios on the basis of past 3-year cumulative returns. Value weighted returns are tracked for 12 months over the second year after portfolio formation, resulting in a series of monthly portfolio returns covering July t+1 to June t+2. This process is repeated every year from 1968 to 2005, providing a series of 456 monthly returns from July 1969 to June 2007. Using this second-year return series, portfolio excess returns are calculated and related to the contemporaneous and lagged NYSE, AMEX and NASDAQ value weighted index excess returns using 445 overlapping annual observations:

$$r_{p,t} = \alpha_{0,p} + \beta_p * r_{m,t} + \beta_{p,-1} * r_{m,t-1} + \epsilon_{p,t},$$

This table reports average parameter estimates and Newey-West corrected t-statistics allowing for twelve lags of autocorrelation.

	$\alpha_{0,p}$				$\beta_{p,-}$			
Group	estimate	\mathbf{t}	estimate	\mathbf{t}	estimate	\mathbf{t}	\bar{R}^2	
Loser	0.010	0.48	1.164	9.68	-0.425	-4.63	0.555	
2	0.046	2.25	0.969	9.85	-0.282	-3.00	0.468	
3	0.034	2.67	0.947	15.97	-0.135	-2.15	0.711	
4	0.028	1.62	0.892	9.80	-0.022	-0.25	0.680	
5	0.037	1.79	0.784	7.21	-0.080	-1.04	0.594	
6	0.039	2.31	0.814	10.54	0.006	0.10	0.660	
7	0.025	2.33	0.965	15.98	0.002	0.05	0.861	
8	0.020	1.73	0.914	13.83	0.065	1.46	0.822	
9	-0.012	-1.05	1.130	22.52	0.099	2.15	0.833	
Winner	-0.028	-2.04	1.316	18.55	0.027	0.39	0.822	

Sorts on Past Performance



The top panel plots $\beta_V = (AN_A\beta_A + GN_G\beta_G)/V$ vs s/C_G , where $V = AN_A + GN_G = V_A + V_G$. A and G are calls on s with exercise prices $C_A = 1, C_G = 100$. $r_f = 0, \sigma^2 T = 1$. $N_A = 1$ and $N_G = 5, 10, 20$. The bottom panel plots the weight in growth options V_G/V vs moneyness s/C_G .